

# WORD PROBLEMS AND ELLs

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Dr. Darlyne de Haan

Presently the Director of Curriculum and Instruction for Math, Science, STEM and Gifted and Talented.

- ❖ Blogger for TESOL- STEM and ELs
- ❖ A former forensic scientist and chemist with more than 20 years of experience in STEM,
- ❖ A recipient and participant of the coveted Fulbright Administrator Program for Fulbright Leaders for Global Schools, a program sponsored by the U.S. Department of State's Bureau of Educational and Cultural Affairs.
- ❖ A strong advocate for changing the face of STEM to reflect the population.
- ❖ Brain Based Science enthusiast
- ❖ Founder of a nonprofit organization-Mad About Science, Inc.
- ❖ Brainbasedscience.com founder
- ❖ Neighborhood-science.com founder



## STEM in ELT: 3 Ways to Seal the Leaky STEM Pipeline

Posted on [4 May 2021](#) by [Darlyne de Haan](#)

The “[Leaky Pipeline](#)” is a metaphor for students’ disproportionate exit from participation in a science, technology, engineering, and mathematics (STEM) content area throughout K–12 school and college, resulting in their underrepresentation in STEM careers. Middle and high school English learners (ELs), students of color, and girls—particularly those from low-income families and schools—are disproportionately excluded or dropped from the STEM pipeline at formative moments in their academic trajectories (Lyon et al., 2012).



Darlyne de Haan

In this blog series, over the next year, I will discuss how to seal the Leaky STEM Pipeline and steps to increase the low number of ELs entering the STEM fields.

Here are three ways of sealing the Leaky Pipeline:

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<http://blog.tesol.org/>

# Upcoming Webinars: 5-Strategies to Improve Math Instruction:

1. Auditory/Oral

2. Visual

3. Instructional

4. Scaffolding

5. Assessment

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5/19/2021

ELLs ARE NOT NECESSARILY  
STRUGGLING LEARNERS; THEY  
ARE LEARNING A NEW  
LANGUAGE...

*THEY ARE BECOMING BILINGUAL*

*Terri Siqueza. Colorín Colorado.org*

# Today's Agenda:

## Working Memory on ELs

A short interactive activity demonstrating what is it and its impact on ELs.

## Comprehension Difficulties in Word Problems

Practice and implement strategies in small groups: manipulating word problems and removing the question.  
Reflecting on the impact this can make for your EL.  
Developing a Critical Eye to Word Problems

## Putting it all Together

Q & A



# Working Memory- It's Impact on ELs

Approximate Age in Range in Years	Capacity of Working Memory in Number of Chunks		
	Minimum	Maximum	Average
Younger than 5	1	3	2
Between 5 and 14	3	7	5
14 and Older	5	9	7

<https://pollev.com/darlynedehaa860>

# Working Memory- It's Impact on EBs

All writing utensils are DOWN!

NBCUSALSDFBIMPH

## Working Memory- It's Impact on EBs

Check how you performed.

NBCUSALSDFBIMPH

<https://pollev.com/darlynedehaa860>

# Working Memory- It's Impact on EBs

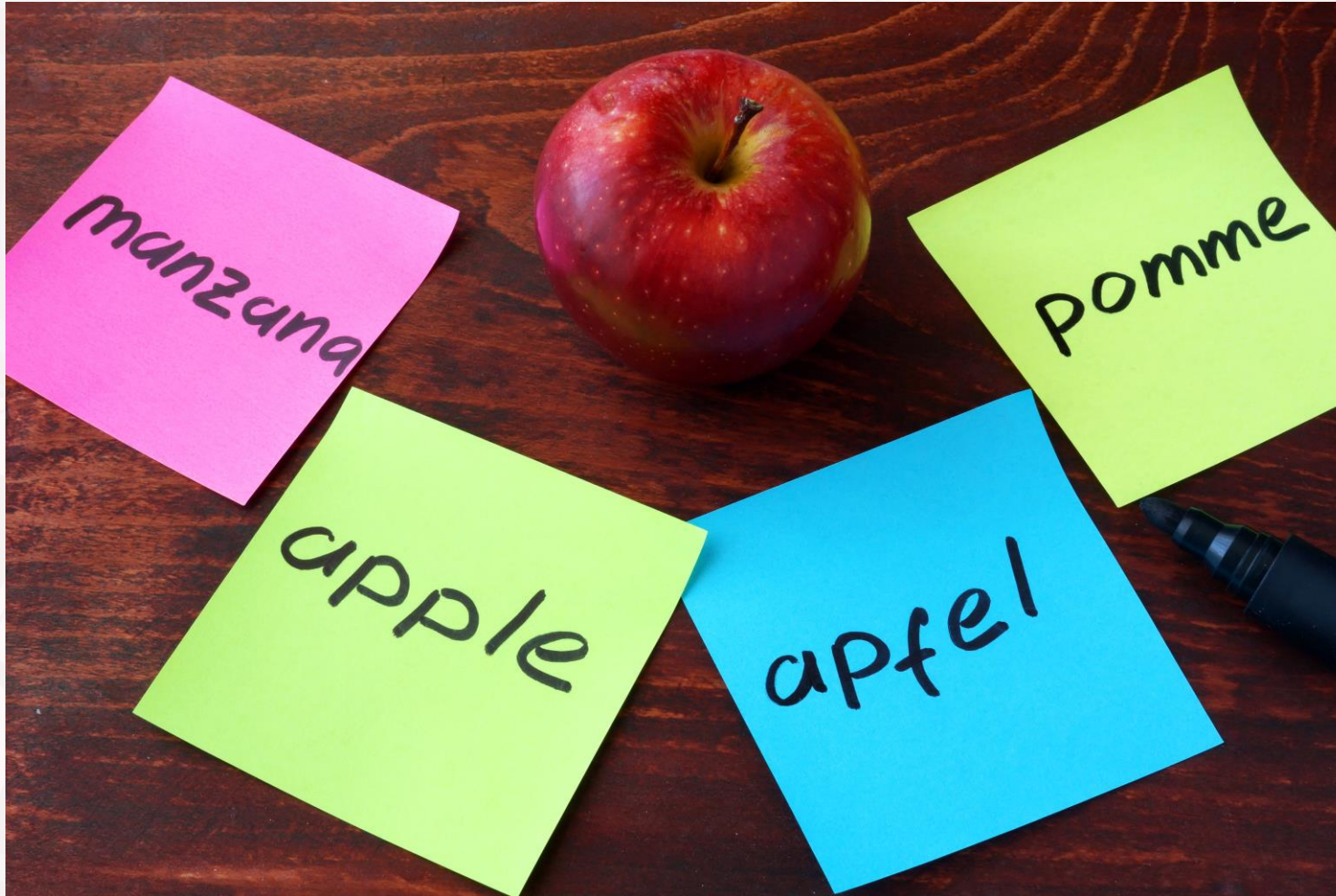
All writing utensils are DOWN!

NBCUSALSDFBIMPH

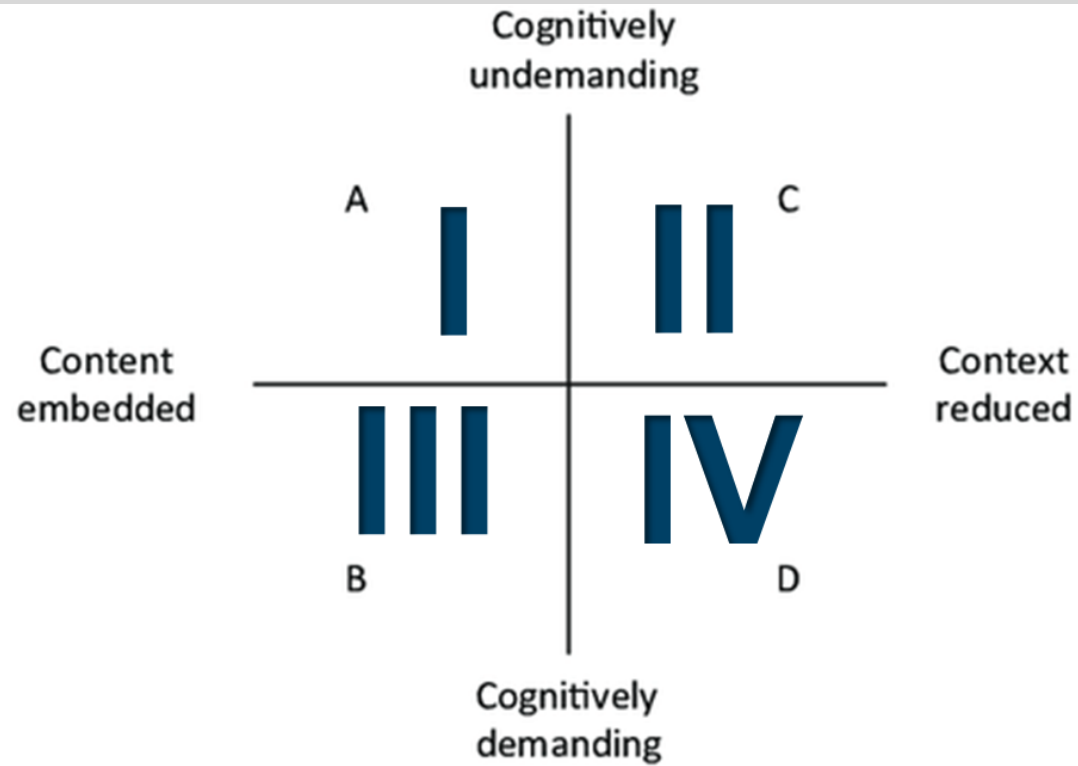
# Working Memory- It's Impact on EBs

Working Memory on  
EBs

What is it and its impact on EBs.  
Interactive Activity



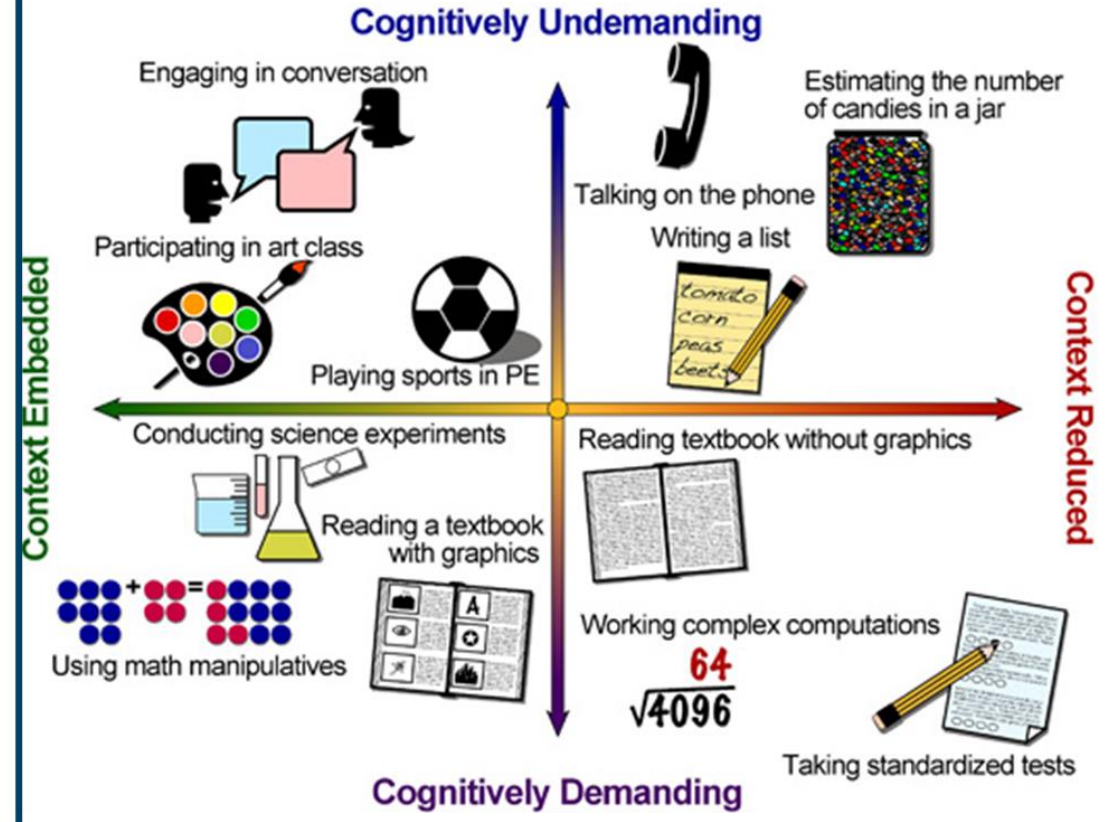
# Cummins' Quadrant



**BICS are cognitively undemanding activities**

A	C
Following directions Face-to-face conversation Buying lunch at school Music, Art, PE classes	Note on the refrigerator Written directions (no visuals) Telephone conversation Oral presentation
B	D
Demonstrations/Experiments Audio-visual assisted lessons Basic math computations Projects and activities Making models/charts/graphs	Standardized Tests Reading/Writing in content areas Math concepts and applications Lecture with few illustrations Textbooks

**... and CALP are cognitively demanding**



A papaya weighs 700 g. A watermelon weighs twice as much.

a) What is the weight of the watermelon?

## Word Problems- It's Impact on ELs

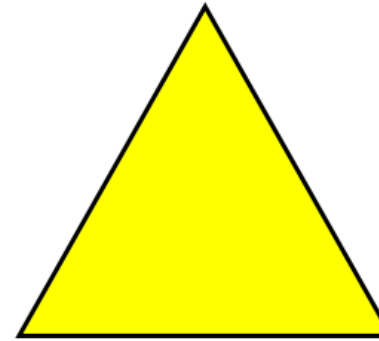
$$\begin{array}{r} 700 \\ \times 2 \\ \hline \end{array}$$

watermelon  $\rightarrow 700 \times 2 = 1400$

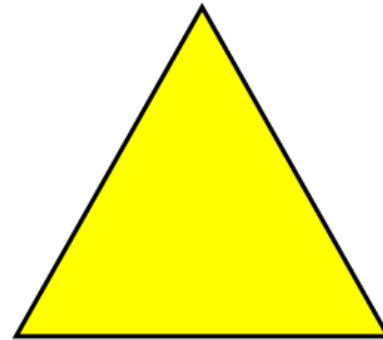
# VISUALIZATION

# acute triangle

acute  
triangle



acute  
triangle



A triangle with no angle  
measuring  $90^\circ$  or more.

# Vocabulary

## STEP 4



### ACTIVITIES

Engage students in activities that add to their knowledge about the word

## STEP 5



### DISCUSS

Students discuss terms with each other

## STEP 6



### GAMES

Involve students in games

"Only confusion will result when the name is demanded before the idea is mastered. Definitions alone rarely throw much light on the ideas they represent. They are usually the end product of much exploration and careful thought."

Joan Countryman,  
Writing to Learn Mathematics, 1992

## STEP 1



### DESCRIBE

Teacher provides an explanation

## STEP 2



### RESTATE

Student restates the explanation

## STEP 3



### DRAW

Students construct a non-linguistic representation

## Comprehension Difficulties in Word Problems

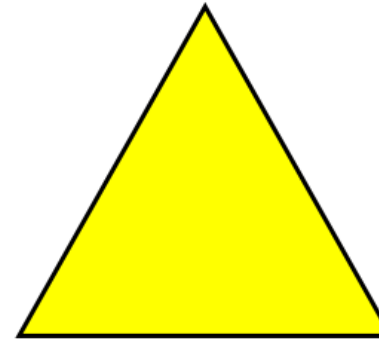
Practice strategies

Manipulating Word Problems

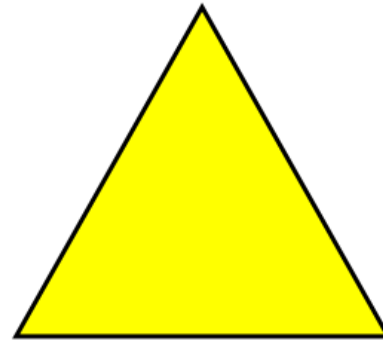


# acute triangle

acute  
triangle



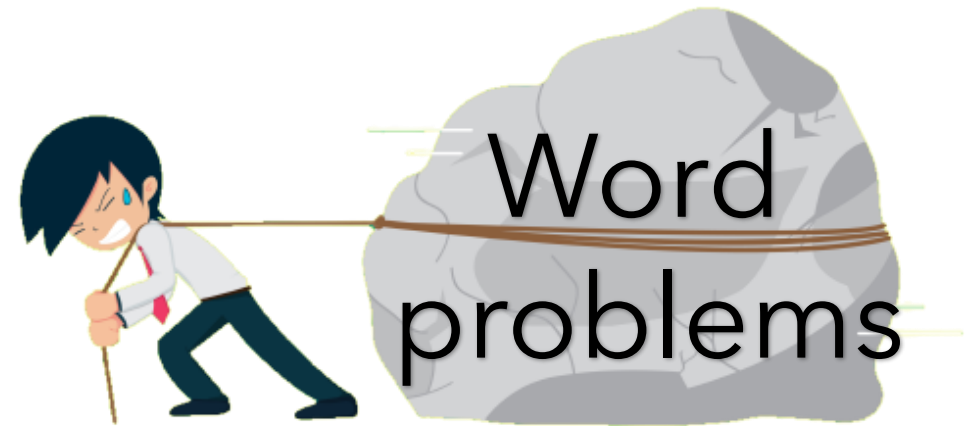
acute  
triangle



A triangle with no angle  
measuring  $90^\circ$  or more.

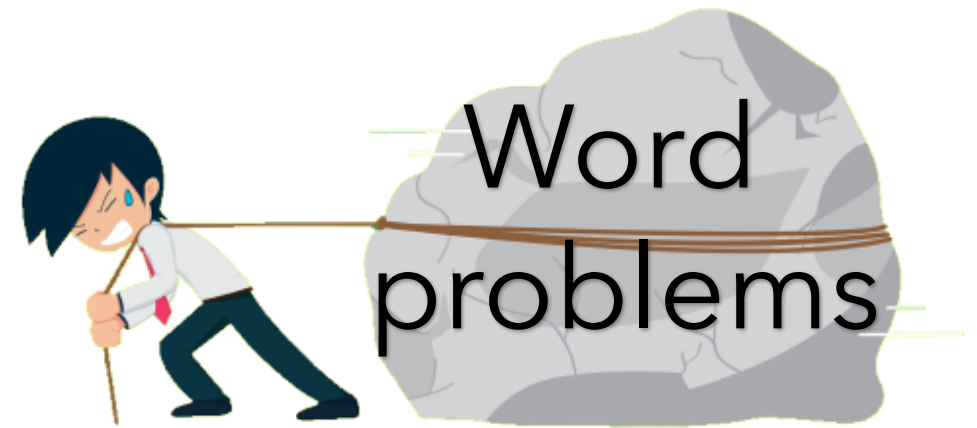
90%

95%



Word problems in mathematics often pose a challenge because they require that students:

- Read and comprehend the text of the problem,
- Identify the question that needs to be answered, and finally;
- Create and solve a numerical equation.



# Vocabulary and Grammar Look-outs

## Quantitative Relationships

- Hardly, higher, last, least, **less**, **many**, most, next, **older**, rarely, scarcely, and **younger**

## Logical Relationships

- Alike, almost, always, because, different from, exactly, **if...then**, never, not quite, opposite of, probably, same, since, unless, and whether

Explain these words using visual aids and manipulatives whenever possible.

# Vocabulary and Grammar Look-outs

## Relationships between two words

- As old as...
- Younger than...
- Greater/less than...
- By what percent is...

## Relationships between two words

- $x$  times as much as...
- **Passive voice** (The bagel was eaten by John...)
- Divided by vs. divided into ex.
- divide 2 by 4 ( $1/2$ ) vs Divide 2 into 4 (2)

Explain these words using visual aids  
and manipulatives whenever possible.

# Vocabulary and Grammar Look-outs

## Pronouns

- If ELLs can't figure out who the pronoun refer back to, they miss out on how the sentences relate to each other.
- The students know all the words, yet not comprehend the meaning.

***Juan has 16 action figures. He gave 9 of them away. How many action figures does he have now?***

## Ellipsis

Ellipsis is when words are left out to tighten the problem.

***All numbers greater than six... is short for  
All numbers (**that are**) greater than six.***

***John earns twice as much money as Robert  
is short for:  
John earns twice as much money as Robert (**earns**).***

Continually look for words that you can replace with  
Higher frequency words.

Comprehension  
Difficulties in Word  
Problems

Practice strategies  
Manipulating Word  
Problems

### Original

1. Mass
2. Estimate
3. Sight
4. How much did she return with?

### New

1. Weight
2. Guess
3. See
4. How much did she have left?

## Rewording of word problems:

## Examples of Grammar and vocabulary issues:


- **If** Peter can type one page of his homework on his computer in 17 minutes, how much time will it take him to type three pages?
- A father is 4 times **as old as** his son. In 20 years, the father will be **twice as old as** his son.
- A sewing machine can sew a set of curtains in  $\frac{3}{4}$  of an hour. It takes a person  $6\frac{1}{2}$  hours to do this same job. How much **less** time is required to do the job by machine?

Another good tool is to teach them to draw or model the problems

## BUCK \$YSTEM:

- **B**= BOX the question
- **U**= Underline the important information
- **C**= Circle the vocabulary
- **K**= Knock out unnecessary words/information

Using journals/graphic organizers to define/draw the meaning of the words.

- **B**=BOX the question
- **U**= Underline the important information
- **C**=Circle the vocabulary
- **K**=Knock out  words/information

## BUCK \$YSTEM: EXAMPLE

At a shop on Times Square three "I ♥ NY" t-shirts sell every 10 minutes for \$19.95 each. Every 45 minutes one Yankee hat sells for \$24.95. The shop is open from 9 am - 9pm everyday. How many t-shirts are sold in a week?

You practice.

Pg.3

- **B**=BOX the question
- **U**= Underline the important information
- **C**=Circle the vocabulary
- **K**=Knock out ~~unimportant~~ words/information

# BUCK \$YSTEM: EXAMPLE

At a shop on Times Square three "I ♥ NY" t-shirts sell every 10 minutes for \$19.99 each. Every 10 minutes one Yankee hat sells for \$19.99. The shop is open from 9 am - 9pm everyday. How many t-shirts are sold in a week.

## NEW WORD PROBLEM

At a shop on Times Square **three** "I ♥ NY" t-shirts sell every **10 minutes**. The shop is open from **9 am - 9pm** everyday. How many t-shirts are sold in a week.

# Practice Rewording Problems:

## Handout

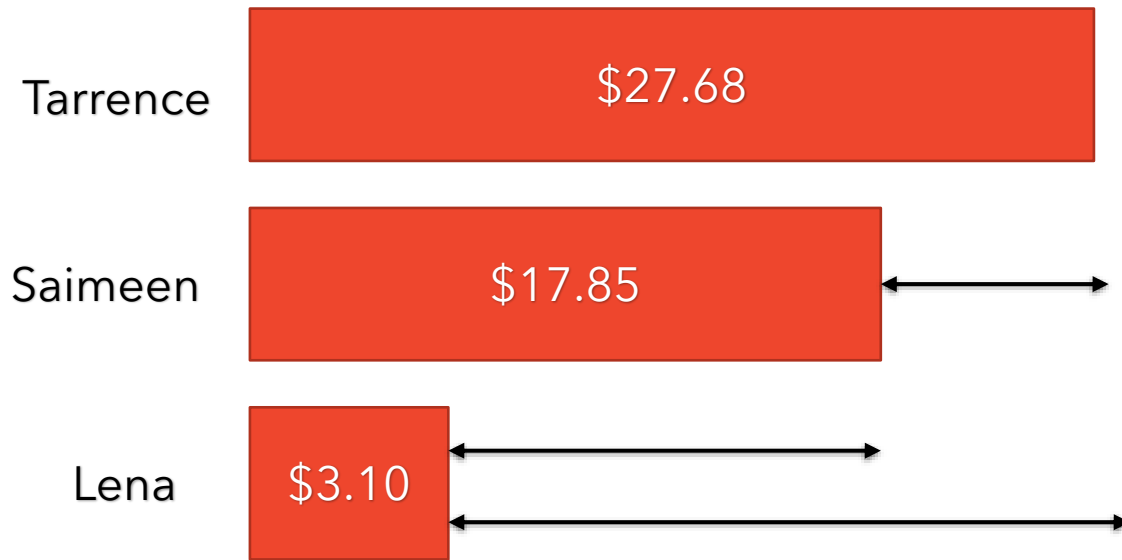
- Group 1: Problem 1 OR 2
- Group 2: Problem 3 OR 4
- Group 3: Problem 5 OR 6
- Group 4: Problem 7 OR 8



Pgs. 4-6



<https://padlet.com/darlynedehaan/xru6rh30gzuzbjld>



Lena has \$3.10,  
Saimeen has \$17.85,  
and Tarrence has  
\$27.68

Model of  
Less than or  
More than.

- Possible Questions:
1. Who has more money?
  2. Put them in order of **least amount** of money to **greatest amount** of money.

- a. Saimeen has \_\_\_\_\_ ¢ **more than** \$17.
- b. Lena spends **half of her money**. Lena has \$ \_\_\_\_\_ **left**.
- c. Saimeen has **7 times as much money as** his brother. Saimeen's brother has \$ \_\_\_\_\_.
- d. Tarrence uses all of his money to buy 8 cupcakes. Each cupcake costs the same amount. How much do 5 cupcakes cost? (Draw another model)

Lena has \$3.10,  
Saimeen has \$17.85,  
and Tarrence has  
\$27.68

Possible Questions:

1. Who has more money?
2. Put them in order of **least amount** of money to **greatest amount** of money.

Looking for

Solution

**I KNOW:**

Samuel will charge \$15 per day to tutor 1 week

**I Need to KNOW:**

\$\_\_\_ if he tutors for 2 weeks

# SENTENCE FRAMES

**PLAN AND WORK:**

\$ charged	15	$\times 14 = 210$
number of days	1	$\times 14 = 14$

1 week = 7 days  
2 weeks = 14 days

**SOLUTION:**

Samuel will charge \$210 to tutor for 2 weeks.

MANEUVERING THE MIDDLE

in 4.0 seconds?

$$\text{speed} = \frac{d}{t} = \frac{112.0 \text{ m}}{4.0 \text{ sec}} = \frac{28 \text{ m}}{\text{sec}}$$

speed of the cheetah is 28 meters per second.

Gi

Re

## Gradual Release and Scaffolds for ELs

### I Do

- Annotate objectives
- Include visuals and videos
- Speak clearly and be explicit
- Use realia (real-life objects)
- Teach mini-lessons
- Model/think-aloud
- Use gestures/TPR
- Use L1 resources

### We Do

- Practice the mini-lesson concept
- Use L1 resources and peers
- Provide sentence stems/frames
- Provide word banks
- Utilize word walls
- Include visuals and videos
- Use gestures/TPR

### They Do

- Use graphic organizers
- Work in pairs or small groups with L1 if needed
- Provide sentence stems/frames
- Provide word banks
- Provide word walls
- Allow translation devices if needed based on proficiency level

### You Do

- Use graphic organizers
- Allow translation devices if needed based on proficiency level
- Provide sentence stems/frames
- Provide word walls
- Allow student use of drawings or visuals to assist in communicating ideas

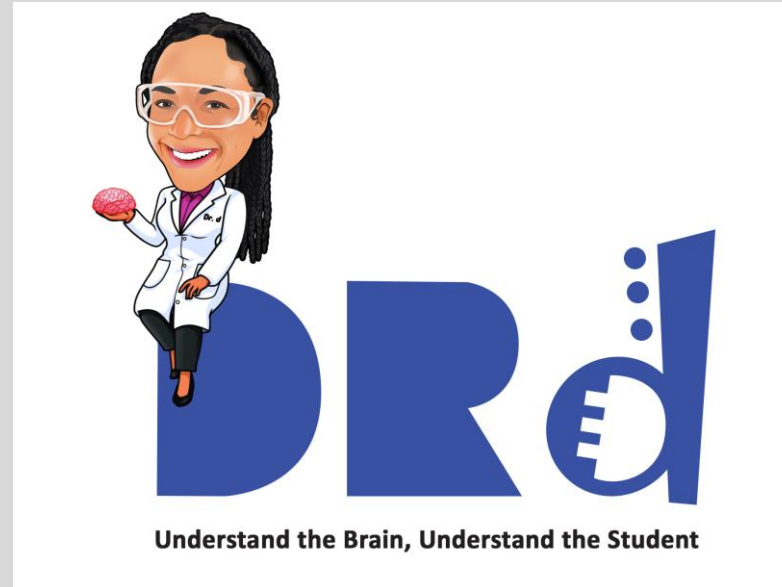
# Gradual Release and Scaffolds for ELs.

# Word Problems:

Story problems are just math problems with words. But for a student who is learning a second (or third) language, words in that new language can create a barrier to understanding. By explicitly teaching English in math class, teachers can help remove the roadblock that often prevents English language learners from making sense of a math word problem and, thus, from solving it. In fact, the challenges that vocabulary, grammar, and syntax pose to English learners can become English language development opportunities in math class.

Always look for opportunities to use strategies, such as repeating, rephrasing, visuals, and offering prompts, that clarify language and make math content accessible.

Thank you! Darlyne de Haan, Ed.D



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## Putting it all Together

Developing a Critical Eye to  
Word Problems

Q & A



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